

Verticals: atmosphere, loading, and reference frames

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GPS Data Processing and Analysis with GAMIT/GLOBK/TRACK
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OVERVIEW

- Atmospheric delay treatment and issues
 - GAMIT setup for different approaches
 - Impacts of atmospheric modeling
- Loading
 - GAMIT setup and some results
- Reference frame realization: Vertical effects
 - Basic approaches
 - Treatment of scale estimates and impact on height estimates

Atmospheric model

- The apriori models used in GAMIT for the atmospheric delays are controlled by the sestbl. entries:
Met obs source = UFL GPT 50 ; hierarchical list
with humidity value at the end; e.g.
RNX UFL GPT 50 ; default GPT 50

DMap = VMF1 ; GMF(default)/VMF1/NMFH;
GMF now invokes GPT2 if gpt.grid is
available (default)

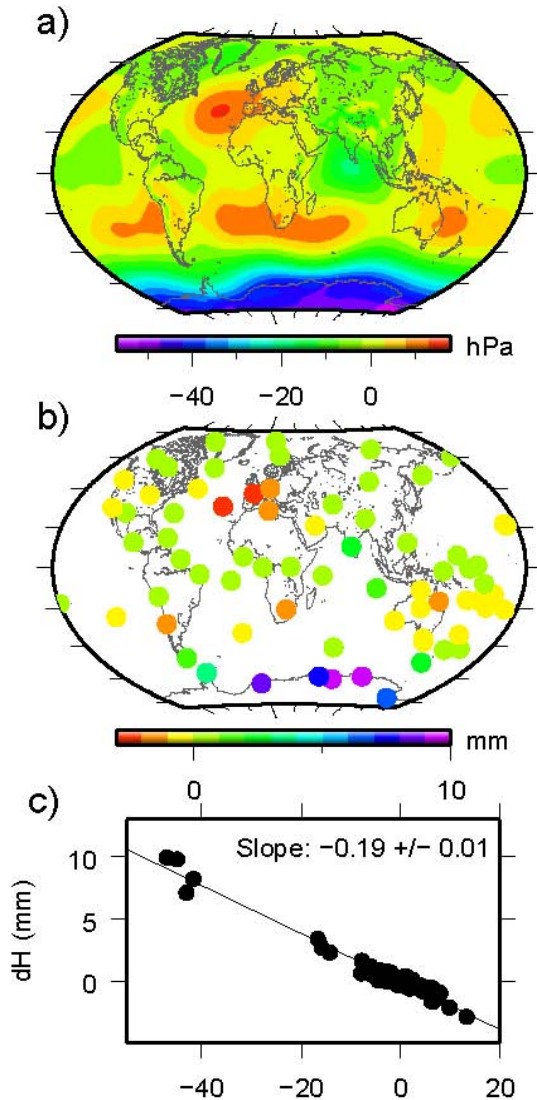
WMap = VMF1 ; GMF(default)/VMF1/NMFW
Use map.list = N ; VMF1 list file with
mapping functions, ZHD, ZWD, P, Pw,
T, Ht

Use map.grid = Y ; VMF1 grid file with
mapping functions and ZHD
- Above would used Vienna mapping functions and met data (surface pressure) from these files. Recommended but not default because of need for grid files.

Setup to use VMF1

- To use VMF1: Met and mapping functions
 - you need to download vmf1grd.YYYY from everest.mit.edu
 - Create links in ~/gg/tables between map.grid.YYYY and the vmf1 files (due to size we assume they may stored in some other location)
 - sh_gamit will automatically link day directory files to your gg/tables files.
- The met source is hierarchical but the mapping functions must specified.

Impact of met source



- Difference between a) surface pressure derived from “standard” sea level pressure and the mean surface pressure derived from the GPT model.
- b) station heights differences using the two sources of a priori pressure.
- c) Relation between a priori pressure differences and height differences. Elevation-dependent weighting was used in the GPS analysis with a minimum elevation angle of 7 deg.

Loading Effects

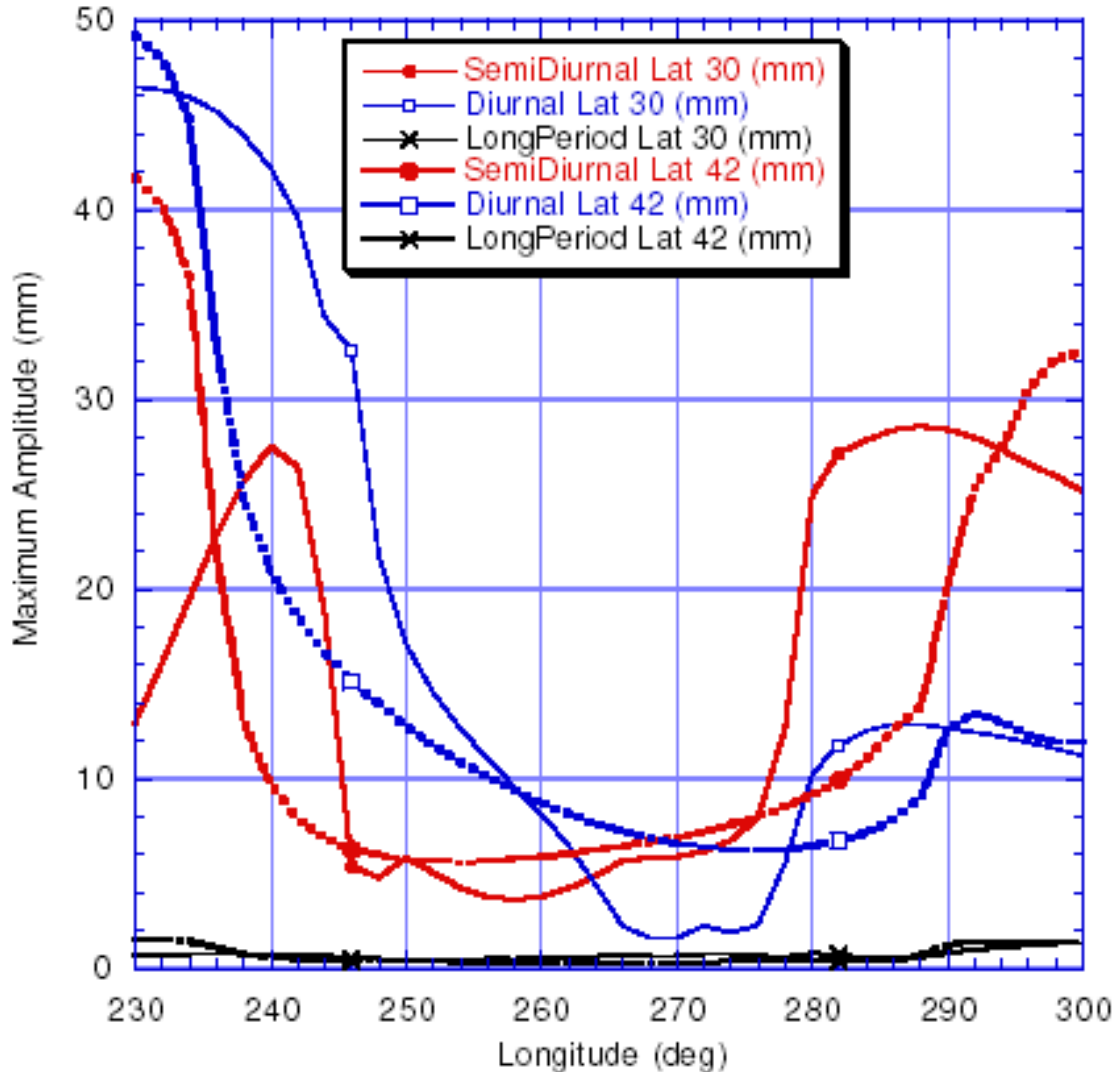
- Invoking in GAMIT; sestbl. Entries
 - Tides applied = 31 ; Binary coded: 1 earth 2 freq-dep 4 pole
8 ocean 16 remove mean for pole tide
; 32 atmosphere ; default = 31
 - Use otl.list = N ; Ocean tidal loading list file from OSO
 - Use otl.grid = Y ; Ocean tidal loading grid file, GAMIT-
format converted from OSO
 - Apply atm loading = N ; Y/N for atmospheric loading
 - Use atml.list = N ; Atmospheric (non-tidal) loading list
file from LU
 - Use atml.grid = N ; Atmospheric (non-tidal) loading grid
file from LU, converted to GAMIT format
 - Use atl.list = N ; Atmospheric tides, list file, not yet
available
 - Use atl.grid = N ; Atmospheric tides, grid file
- Default settings. Consistent with IGS ITRF2014 contribution (i.e., no non-tidal loading applied).

To apply “Tidal” loading

- Ocean tidal loading is needed. Link otl.grid in gg/tables to otl_FES2004.grid (download from everest.mit.edu; not included in standard tar files due to size). Close to the coast in complicated regions, list values specific to a location might be better. Be careful that nearby sites don't from different sources.
- “Tidal” atmospheric pressure loading atl.grid has diurnal and semidiurnal S1 and S2 load. Nominally removed from 6hr tabular atmospheric loading values before interpolation (usefulness of this model is not clear --- mostly harmless).

Ocean loading magnitudes

Radial Ocean Loading Effects



Locations at "corners"

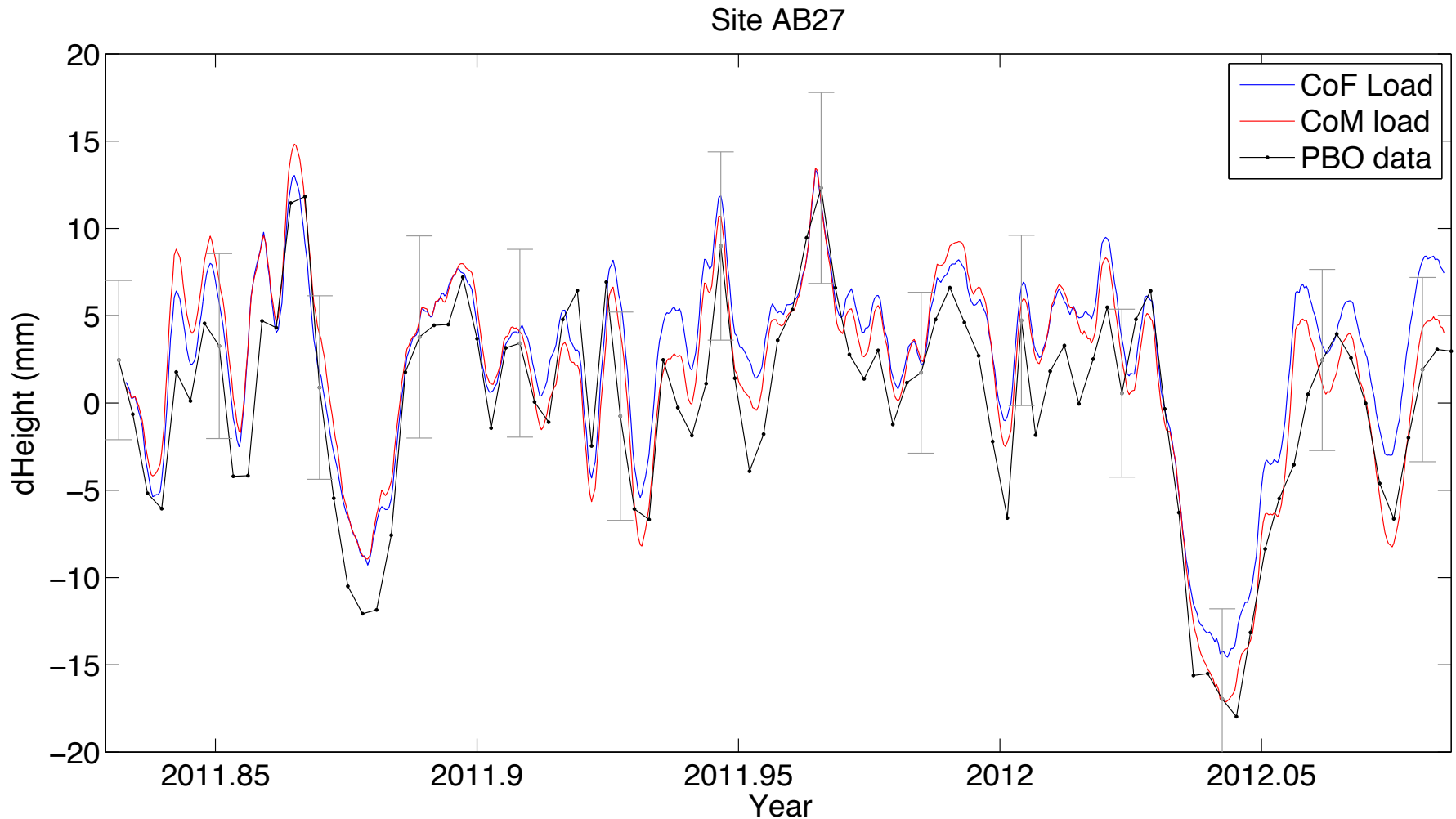
WES2	288.5	42.6
ALBH	236.5	48.4
RICH	279.6	25.6
SIO	242.8	32.8

To apply non-tidal loading

- Set sestbl. for atml.grid and link atml.grid.YYYY in gg/tables to the appropriate grid files. (atml.list option currently not used).
- When linking atml.grid, there are choices of loading types (files available in GRIDS on everest.mit.edu)
 - atmdisp_cm.YYYY: Center of mass, 6hr raw data
 - atmfilt_cm.YYYY: Center of mass, filtered to remove periods less than ~1.2 day. Should be used with S1/S2 atl.grid file.
 - Center of figure (cf) and center of earth (ce) frames are available also (these frames are almost identical).
- When working in current year, near realtime, updated files from everest need to be downloaded regularly.
- Atml Loading applied in GAMIT can be removed in GLOBK with the appl_mod command.
- Hydrology loading is supported in the file formats but is currently not implemented in GAMIT.

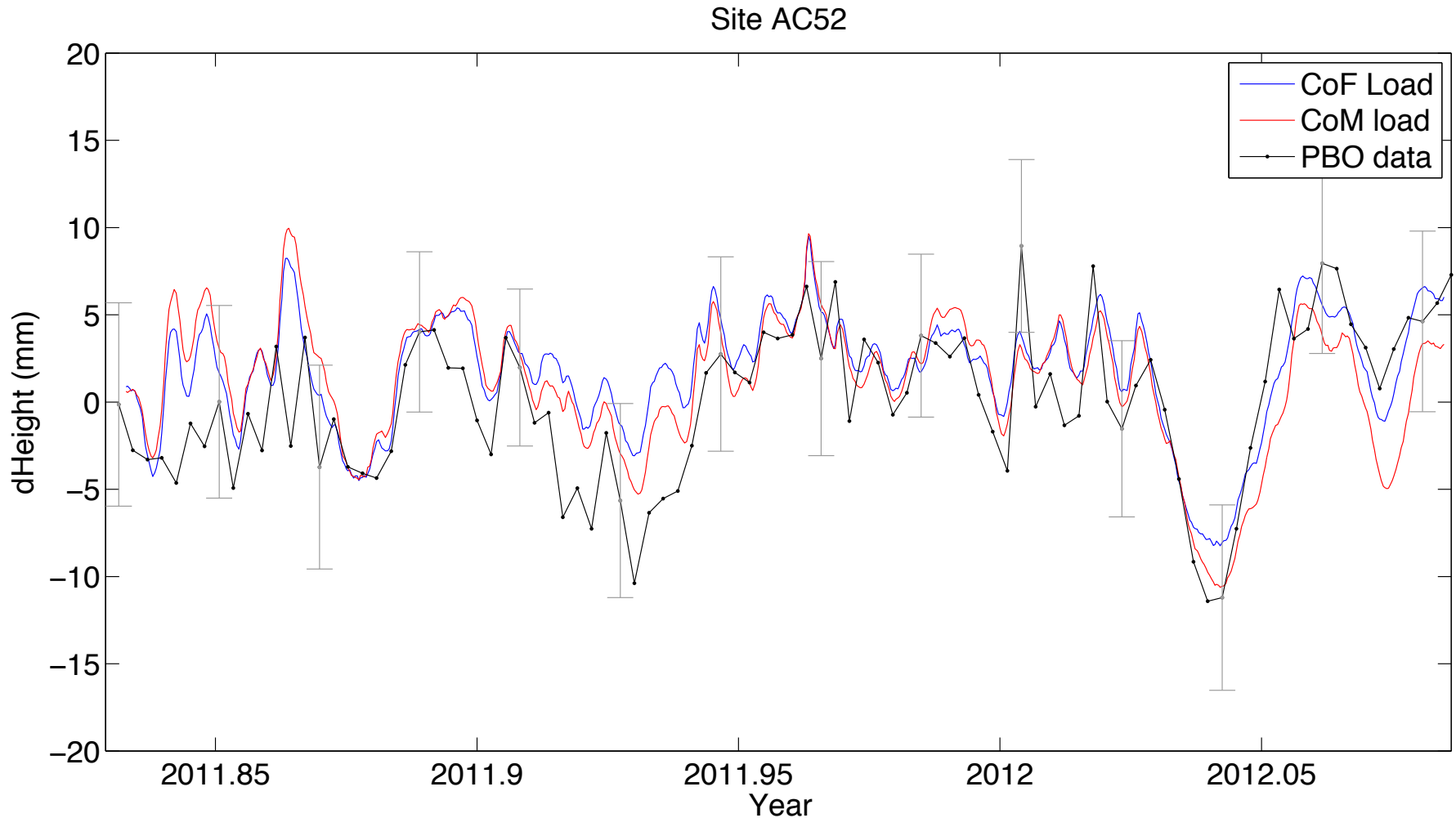
Example: Atmospheric load

- AB27 in central Alaska



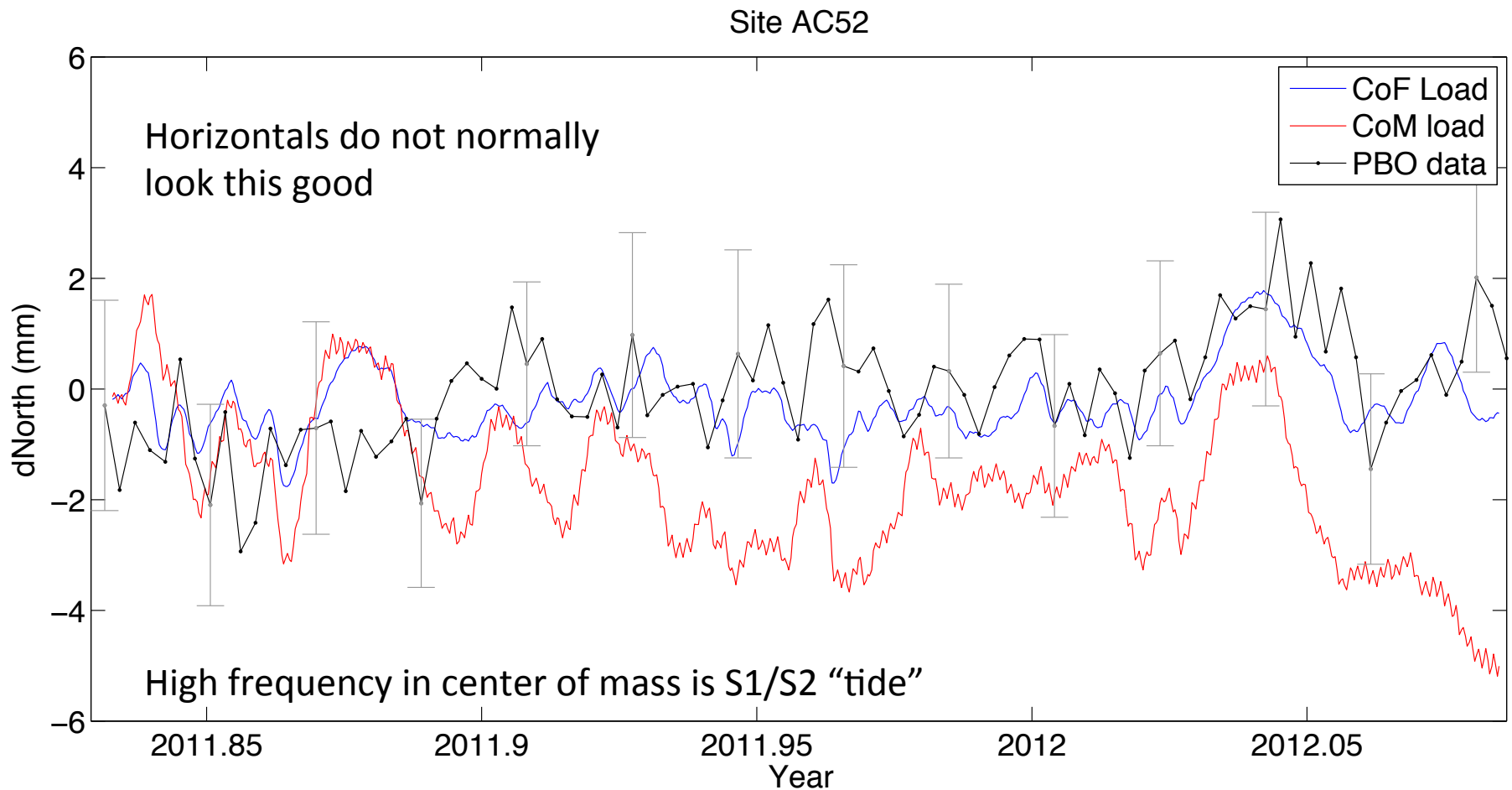
Example: Atmospheric load

- AC52 in Southern coastal Alaska



Example: Atmospheric load

- AC52 in Southern coastal Alaska: North



Basic issues in reference frame realization

- Concept is to align the estimated site positions and possibly velocity to a set of well defined locations that have physical significance for the analysis being performed (e.g., PBO we align to a realization of the North America plate based on ITRF2008).
- GLORG is the module which does this and computes the covariance matrix of the aligned solution in the reference frame chosen.
- Transformation is often called an N-parameter Helmert transformation:
 - N=3 translation only (could also be just rotation)
 - N=6 translation and rotation
 - N=7 translation, rotation and scale
- In GLOBK analyses, you need to decide
 - How many parameters (3/6/7)
 - Sites to use to determine the parameters (sh_gen_stats)
 - Values of the positions/velocities of the reference frame sites
 - Weight to be given to heights in computing the transformation parameters (CND_HGTV command; first two arguments for position and velocity).

Choices of reference frame

- Choose your reference frame based on your geophysical objectives
 - Velocities in ITRF are difficult to interpret visually from a geophysical perspective
 - Local surroundings of a volcano
 - One side of a fault
 - Upper plate of a subduction zone
- Major plate reference frame
 - Major plates are often chosen to conform with conventional perspectives of velocity solutions
 - Relative to Eurasia, Nubia, North America, South America, etc.
 - But don't feel restricted by this. Sometimes your geophysical discussion is best visualized relative to any stable boundary of a deforming region
- Regional reference frame
 - Central Valley of California, non-deforming part of Anatolia, smaller coherent regions, etc
- Local reference frame
 - Sites near but outside the influence of a volcano, geothermal field, etc.

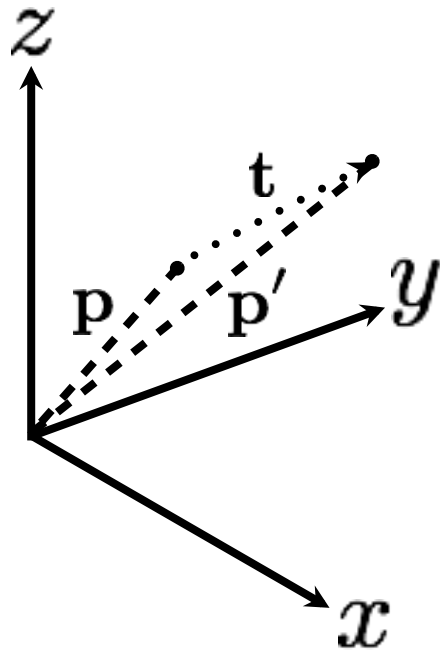
Ways to define a reference frame

- Create an apr-file for use by glorg
 1. Apply known rotation rate to apr-file (e.g. `itr08_comb.apr` → `itr08_comb_eura.apr`)
 2. Zero velocity apr-file records (and iterate using `sh_exglk` to create updated apr-file)
- Define set of sites (must be included in GAMIT processing or other H-file input to GLOBK) which define stable region
 3. `plate` in globk command file

Reference frame implementation

- Any vector may be mapped from one co-ordinate system to another by the application of
 - Translation (affects position of co-ordinate origin)
 - Rotation (affects orientation of co-ordinate axes)
 - Scale (affects length of co-ordinate axes)

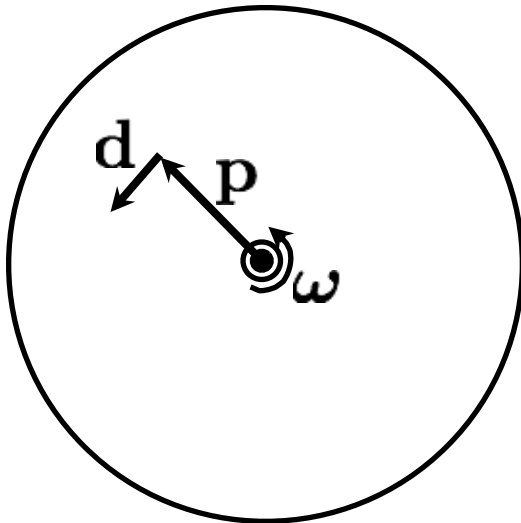
1: Translation



$$\mathbf{p}' = \mathbf{p} + \mathbf{t}$$
$$\begin{pmatrix} p'_x \\ p'_y \\ p'_z \end{pmatrix} = \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \\ t_z \end{pmatrix}$$

2: Rotation

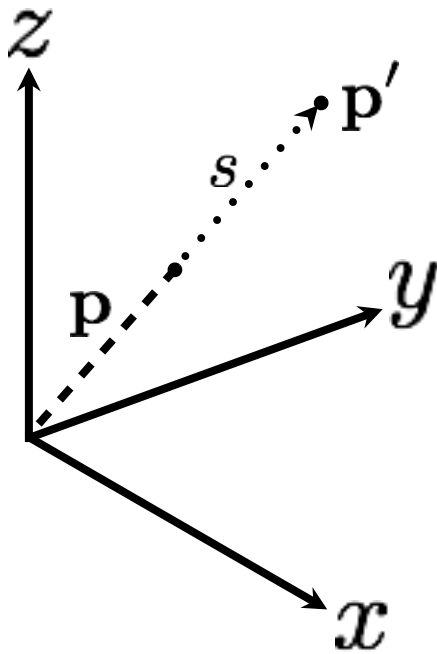
- Rotation vector, $\boldsymbol{\omega}$, is defined as in the direction of the rotation axis with length equal to the magnitude of angular rotation
- Displacement (or velocity) vector then makes a right-handed triplet with the rotation vector, $\boldsymbol{\omega}$, and radial vector, \boldsymbol{p} .



$$\begin{aligned}\boldsymbol{d} &= \boldsymbol{\omega} \times \boldsymbol{p} \\ &= \begin{pmatrix} \omega_x \\ \omega_y \\ \omega_z \end{pmatrix} \times \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}\end{aligned}$$

$$\begin{aligned}\boldsymbol{d} &= \mathbf{R}\boldsymbol{p} \\ &= \begin{pmatrix} 0 & -\omega_z & \omega_y \\ \omega_z & 0 & -\omega_x \\ -\omega_y & \omega_x & 0 \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}\end{aligned}$$

3: Scale



$$\mathbf{p}' = \mathbf{p} + s\mathbf{p}$$
$$\begin{pmatrix} p'_x \\ p'_y \\ p'_z \end{pmatrix} = \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix} + s \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}$$

Helmert transformation

- Position

$$\mathbf{p}' = \mathbf{p} + \mathbf{t} + \mathbf{R}\mathbf{p} + s\mathbf{p}$$

$$\begin{pmatrix} p'_x \\ p'_y \\ p'_z \end{pmatrix} = \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix} + \begin{pmatrix} t_x \\ t_y \\ t_z \end{pmatrix} + \begin{pmatrix} s & -\omega_z & \omega_y \\ \omega_z & s & -\omega_x \\ -\omega_y & \omega_x & s \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}$$

- Velocity

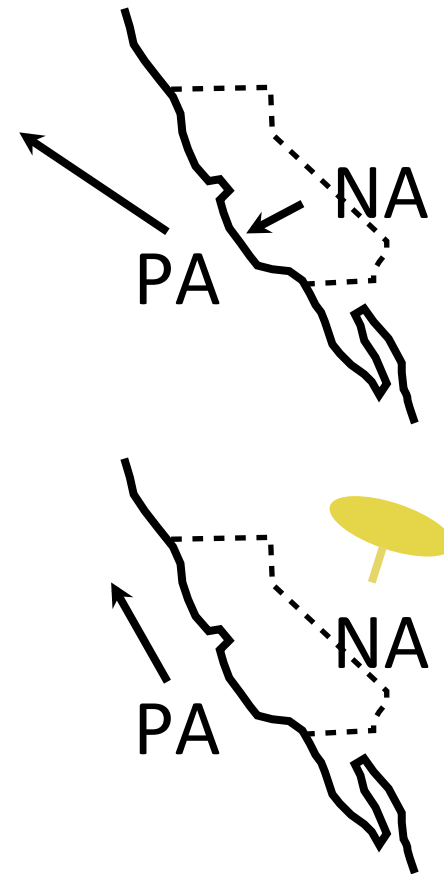
$$\mathbf{v}' = \mathbf{v} + \dot{\mathbf{t}} + \cancel{\mathbf{R}\mathbf{v}} + \dot{\mathbf{R}}\mathbf{p} + \cancel{s\mathbf{v}} + \dot{s}\mathbf{p}$$

$$\begin{pmatrix} v'_x \\ v'_y \\ v'_z \end{pmatrix} = \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} + \begin{pmatrix} \dot{t}_x \\ \dot{t}_y \\ \dot{t}_z \end{pmatrix} + \begin{pmatrix} s & -\omega_z & \omega_y \\ \omega_z & s & -\omega_x \\ -\omega_y & \omega_x & s \end{pmatrix} \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} + \begin{pmatrix} \dot{s} & -\dot{\omega}_z & \dot{\omega}_y \\ \dot{\omega}_z & \dot{s} & -\dot{\omega}_x \\ -\dot{\omega}_y & \dot{\omega}_x & \dot{s} \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}$$

- Usually, the terms $\mathbf{R}\mathbf{v}$ and $s\mathbf{v}$ are very small and can be neglected ($< 10^{-6}$ rad \times < 0.1 m/yr and < 0.1 ppb \times < 0.1 m/yr, respectively)

Examples

- Expressing velocities in ITRF is not very meaningful or useful when we want to look at the deformation at a plate boundary, e.g. the San Andreas Fault system
- Better to look at velocities with one side “fixed” so we can see what the other side is doing relative to it



What does “with respect to” mean?

- Horizontal motions are restricted to the surface of the Earth, therefore the Helmert transformation may not contain translation or scaling of position terms

$$\mathbf{v}' = \mathbf{v} + \cancel{\dot{\mathbf{t}}} + \cancel{\mathbf{R}}\mathbf{v} + \mathbf{R}\dot{\mathbf{p}} + \cancel{s}\mathbf{v} + \cancel{\dot{s}}\mathbf{p}$$

$$\begin{pmatrix} v'_x \\ v'_y \\ v'_z \end{pmatrix} = \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} + \begin{pmatrix} \dot{t}_x \\ \dot{t}_y \\ \dot{t}_z \end{pmatrix} + \begin{pmatrix} s & -\omega_z & \omega_y \\ \omega_z & s & -\omega_x \\ -\omega_y & \omega_x & s \end{pmatrix} \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} + \begin{pmatrix} \dot{s} & -\dot{\omega}_z & \dot{\omega}_y \\ \dot{\omega}_z & \dot{s} & -\dot{\omega}_x \\ -\dot{\omega}_y & \dot{\omega}_x & \dot{s} \end{pmatrix} \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix}$$

1. Set \mathbf{v}' to zero for all sites that you wish to estimate all other velocities with respect to
2. Estimate the best-fit transformation parameters, e.g. by least squares estimation, to achieve this minimization of velocities in a region
3. Apply the estimated transformation to all velocities
4. All velocities are now “with respect to” the chosen subset
5. The subset could be, for instance, all on one tectonic plate, or any given region from which you wish to see the deformation

Reference frames in Geodetic Analyses

- Output from GAMIT
 - Loosely constrained solutions
 - Relative position well determined, “Absolute position” weakly defined
 - Need a procedure to expressed coordinates in a well defined reference frame
- Two aspects
 - Theoretical (e.g., rigid block, mantle-fixed, no-net-rotation of plates)
 - Realization through a set of coordinates and velocities
 - “finite constraints” : a priori sigmas on site coordinates
 - “generalized constraints” : minimize coordinate residuals while adjusting translation, rotation, and scale parameters
- Three considerations in data processing and analysis
 - Consistent with GPS orbits and EOP (NNR)
 - not an issue if network small or if orbits and EOP estimated
 - Physically meaningful frame in which to visualize site motions
 - Robust realization for velocities and/or time series

Frame definition with finite constraints

- Applied in globk (glorg not called): We do not recommend this approach since it is sensitive to over-constraints that can distort velocities and positions

- Example:

```
apr_file itr08.apr
```

```
apr_neu all 10 10 10 1 1 1
```

```
apr_neu algo .005 005 .010 .001 .001 .003
```

```
apr_neu pie1 .002 005 .010 .001 .001 .003
```

```
apr_neu drao .005 005 .010 .002 .002 .005
```

```
...
```

- Most useful when only one or two reference sites or very local area.
- Disadvantage for large networks is that bad a priori coordinates or bad data from a reference site can distort the network

Frame definition with generalized constraints

- Applied in glorg: minimize residuals of reference sites while estimating translation, rotation, and/or scale (3 -7 parameters)

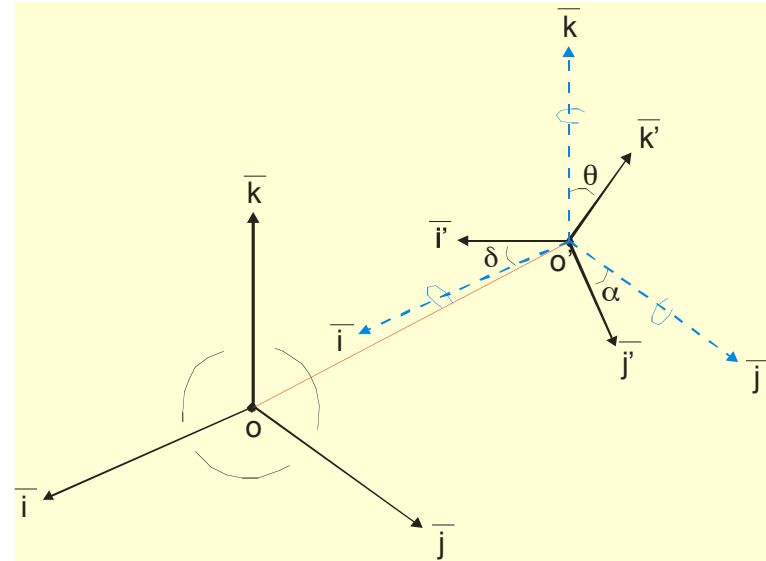
```
apr_file itr08.apr
```

```
pos_org xtran ytran ztran xrot yrot zrot
```

```
stab_site algo pie1 drao ...
```

```
cnd_hgtv 10 10 0.8 3.
```

```
stab_it 4 0.5 2.5
```



- All reference coordinates free to adjust (anomalies more apparent); outliers are iteratively removed by glorg
- Network can translate and rotate but not distort
- Works best with strong redundancy (number and [if rotation] geometry of coordinates exceeds number of parameters iloadng effects)

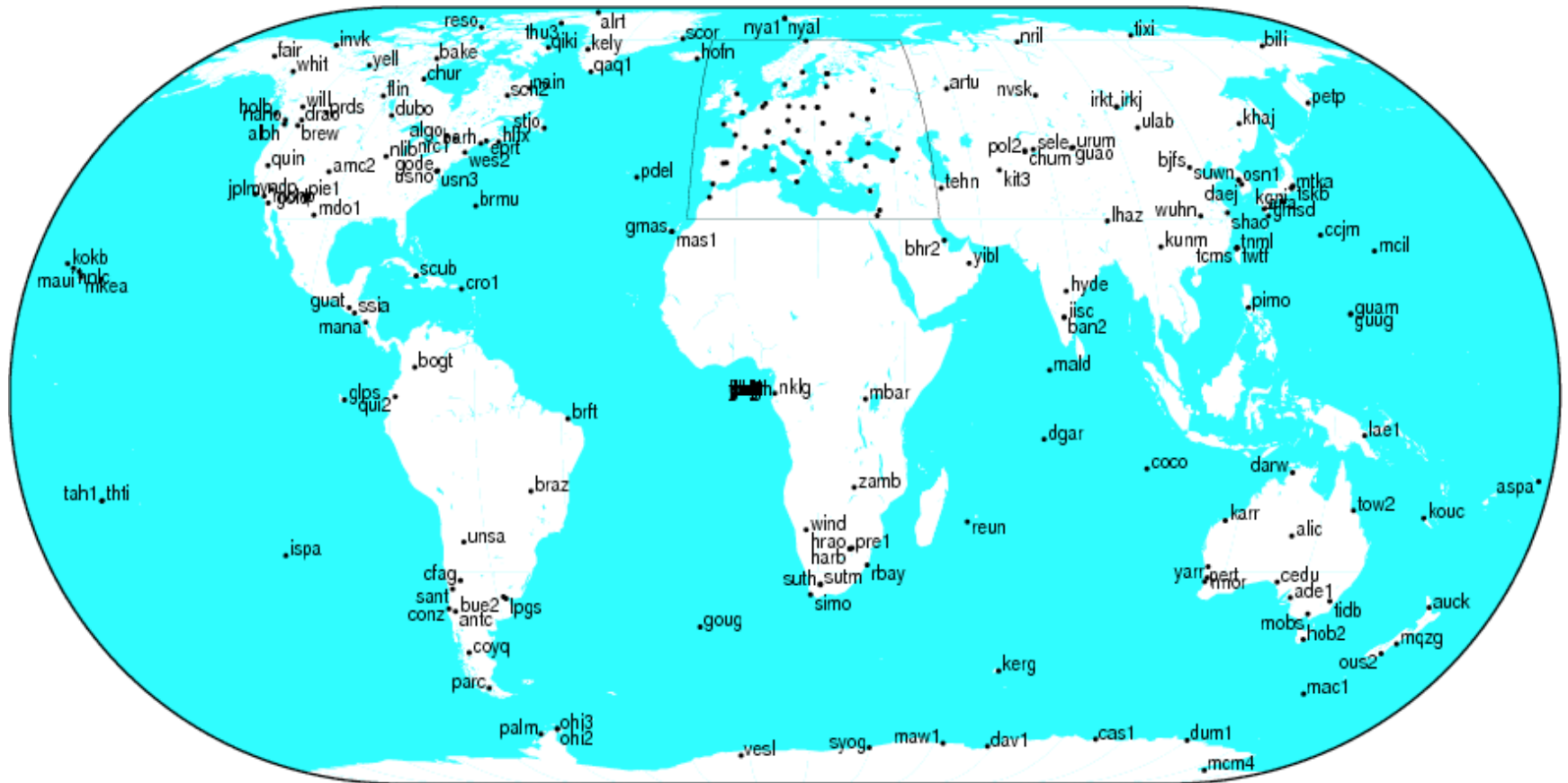
Stabilization using a Global Set of Sites

- Use 40 or more sites with good velocities determined in the ITRF2008 frame
- The `itr08_comb.apr` file, when used together with `itr08_comb.eq` to account consistently for instrumental changes over time, provides the widest choice of sites, 1992-2013.
- Combining your solution with the MIT or SOPAC global h-files offer access to over 100 sites without having to include them in your GAMIT processing.
 - You need just 4-6 common sites, which should be of high quality but need not be well known in ITRF2008 since these “tie” sites do not need to be in your frame-realization list.
- For global ITRF stabilization, you can use the hierarchical list `igb08_heirarchy.stab_site` in `gg/tables`
- Although a global frame may be a convenient way to do the stabilization, it is usually not necessary for regional studies.

Stabilization using Regional or Local Sites

- If your area of study has a robust cGPS network (10 or more well-distributed sites) with accurate a priori velocities, then glorg stabilization is robust and little thought is involved (glorg will automatically discard the one or two sites which may be weak or inconsistent)
- If your region is short on cGPS stations with well-known coordinates, you will need to think carefully about the choice of sites to include in your solution and use the initial stabilization. A stabilization site should have
 - high quality data over the full span of your study
 - coordinates well-known in ITRF2008
 - Provide symmetric coverage around your study area (except that if the region is small enough, a translation-only stabilization may be possible and distribution is less important)

IGS (IGb08) reference frame network

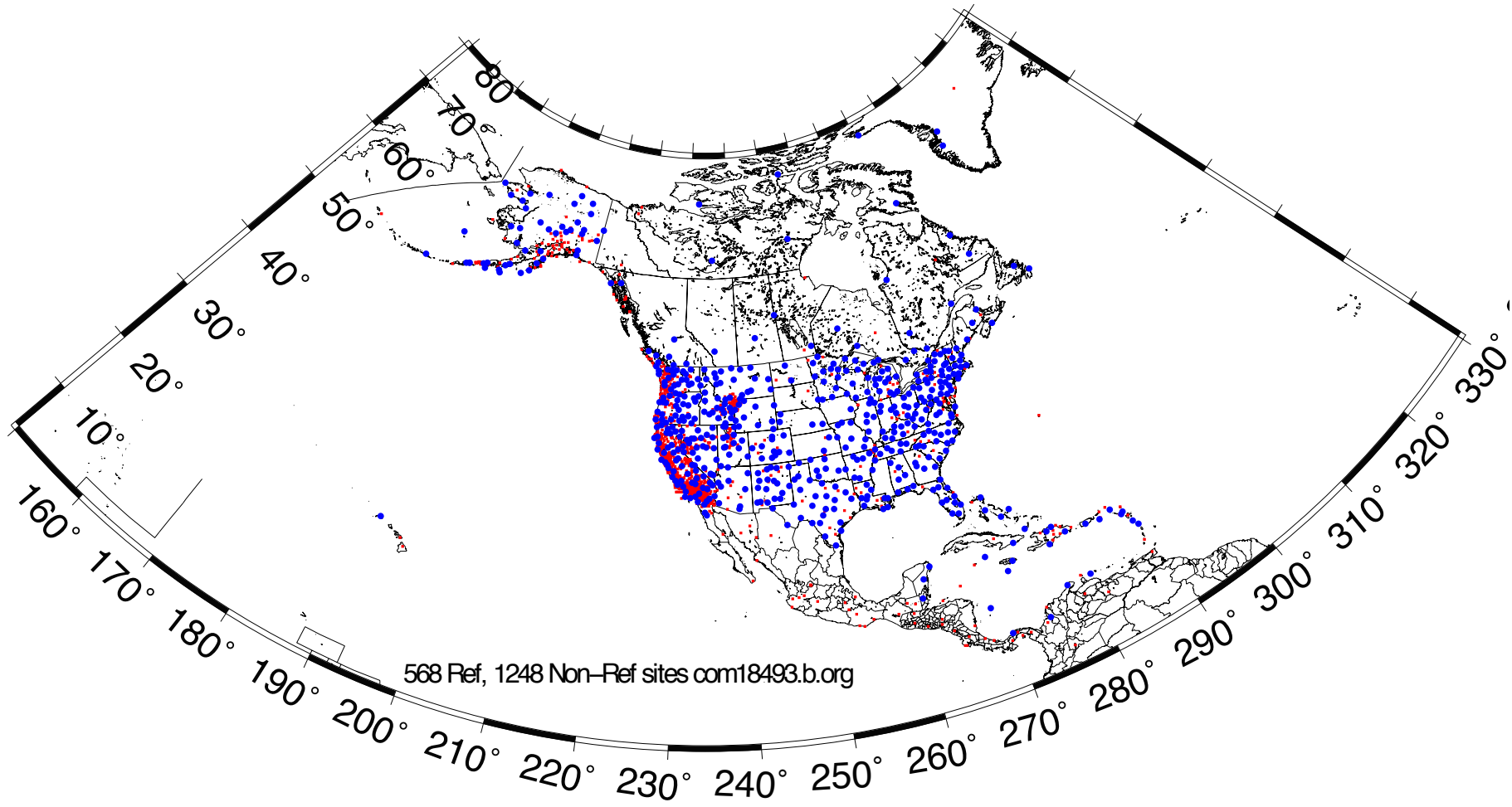


© IGS 2013 Jul 09 16:46:07

<http://igscb.jpl.nasa.gov/network/refframe.html>

Frame realization sites for PBO

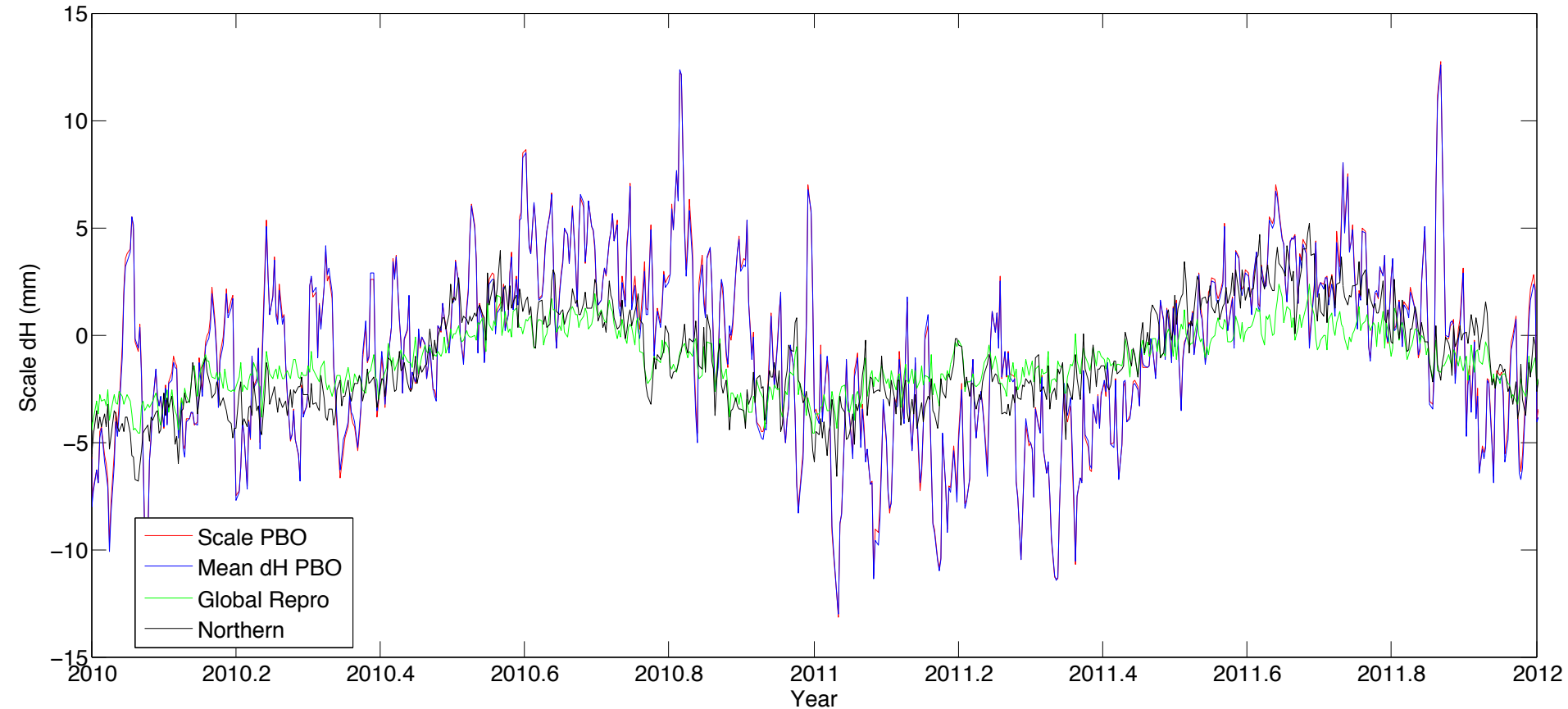
- PBO used an hierarchical list based on 500km site spacing (sh_gen_stat stabrad option). (Blue dots)



Issues with Estimating Scale

- Many GPS analyses, automatically include scale when aligning reference frames. Since the Earth is almost spherical, scale changes are directly proportional to the average height difference between the reference site coordinates and their apriori values.
- When comparing and analyzing height changes, how scale is treated directly effects the results. Aspects of this issue are discussed in a white paper that should be available shortly from the GAGE analysis documentation at UNAVCO.
- Scale estimates are related the mean height differences over the reference sites. Should this be removed or not is an open question.
- Scale estimates on next slide show magnitude of effect for the PBO network.

PBO network scale estimates



PBO network estimates compared to global estimates converted to average height differences (6317 km Earth). Spikes in winter are often due to Alaskan sites.

Use of Global binary H-files

- Include global h-files ... or not ? For post-2000 data not needed for orbits
- Advantages
 - Access to a large number of sites for frame definition
 - Can (should) allow adjustment to orbits and EOP
 - Eases computational burden
- Disadvantages
 - Must use (mostly) the same models as the global processing
 - Orbits implied by the global data worse than IGSF. Once-per-revolution radiation model parameters (loose in global h-files) should be treated carefully.
 - Some bad data may be included in global h-files (can remove)
 - Greater data storage burden
- MIT hfiles available at ftp://everest.mit.edu/pub/MIT_GLL/HYY
When using MIT files, add apr_svant all F F F to globk command file to fix the satellite antenna offsets

Velocities and Time Series

- The criteria for stabilization are different for velocity solutions and time series
- Velocity solutions:
 - Physical reference is important
 - Not so sensitive to station dropout (solution holds the frame together)
- Time series:
 - Physical reference is not important
 - Sensitive to station dropout
 - Best representation of the statistics of the velocity solution is stabilization using ALL the well-determined sites from the velocity solution, now in a common frame

a priori coordinate files

- We now distribute, and encourage GAMITeers to use, a set of apr-files that are a concatenated set of coordinates for all sites that are, in some present or past version, formally defined in the ITRF (531 sites or 891 including those in IGS cumulative solution)
- Found in ~/gg/tables/ and use in apr_file command or glorg command file
- These are also rotated to major plates using the Euler poles of ITRF2008-PMM (Altamimi *et al.*, 2012)
 - itr08_comb_amur.apr (relative to Amurian plate)
 - itr08_comb_anta.apr (Antarctica)
 - itr08_comb_arab.apr (Arabia)
 - itr08_comb_aust.apr (Australia)
 - itr08_comb_carb.apr (Caribbean)
 - itr08_comb_eura.apr (Eurasia)
 - itr08_comb_indi.apr (India)
 - itr08_comb_na12.apr (North America, after Blewitt et al., 2013)
 - itr08_comb_nazc.apr (Nazca)
 - itr08_comb_noam.apr (North America)
 - itr08_comb_nubi.apr (Nubia)
 - itr08_comb_nu13.apr (Nubia, after Saria et al., 2013)
 - itr08_comb_pcfc.apr (Pacific)
 - itr08_comb_soam.apr (South America)
 - itr08_comb_soma.apr (Somalia)
 - itr08_comb_sund.apr (Sunda)

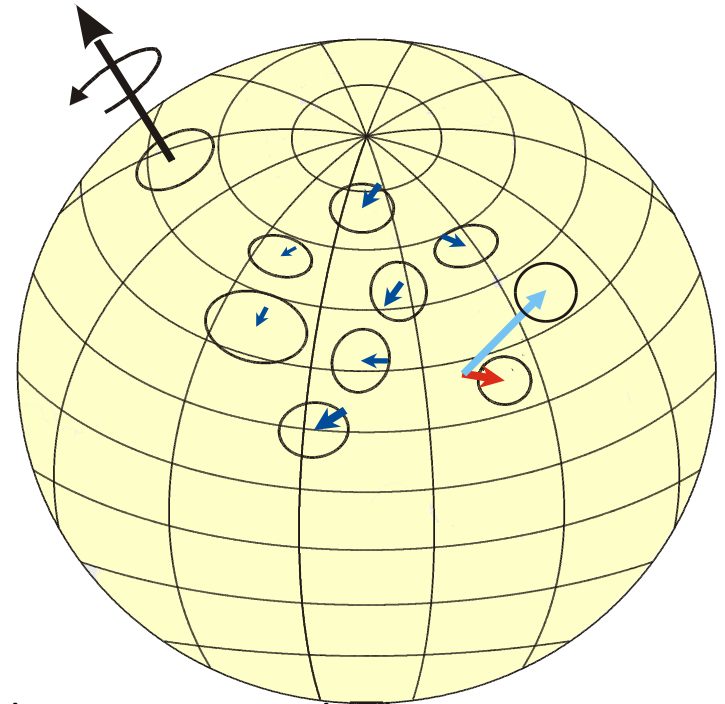
Referencing to a horizontal block ('plate')

Applied in glorg: first stabilize in the usual way with respect to a reference set of coordinates and velocities (e.g. ITRF-NNR), then define one or more 'rigid' blocks

```
apr_file itr08.apr  
pos_org xtran ytran ztran xrot yrot zrot  
stab_site algo pie1 nlib drao gold sni1 mkea chat  
cnd_hgtv 10 10 0.8 3.  
plate noam algo pie1 nlib  
plate pcfc sni1 mkea chat
```

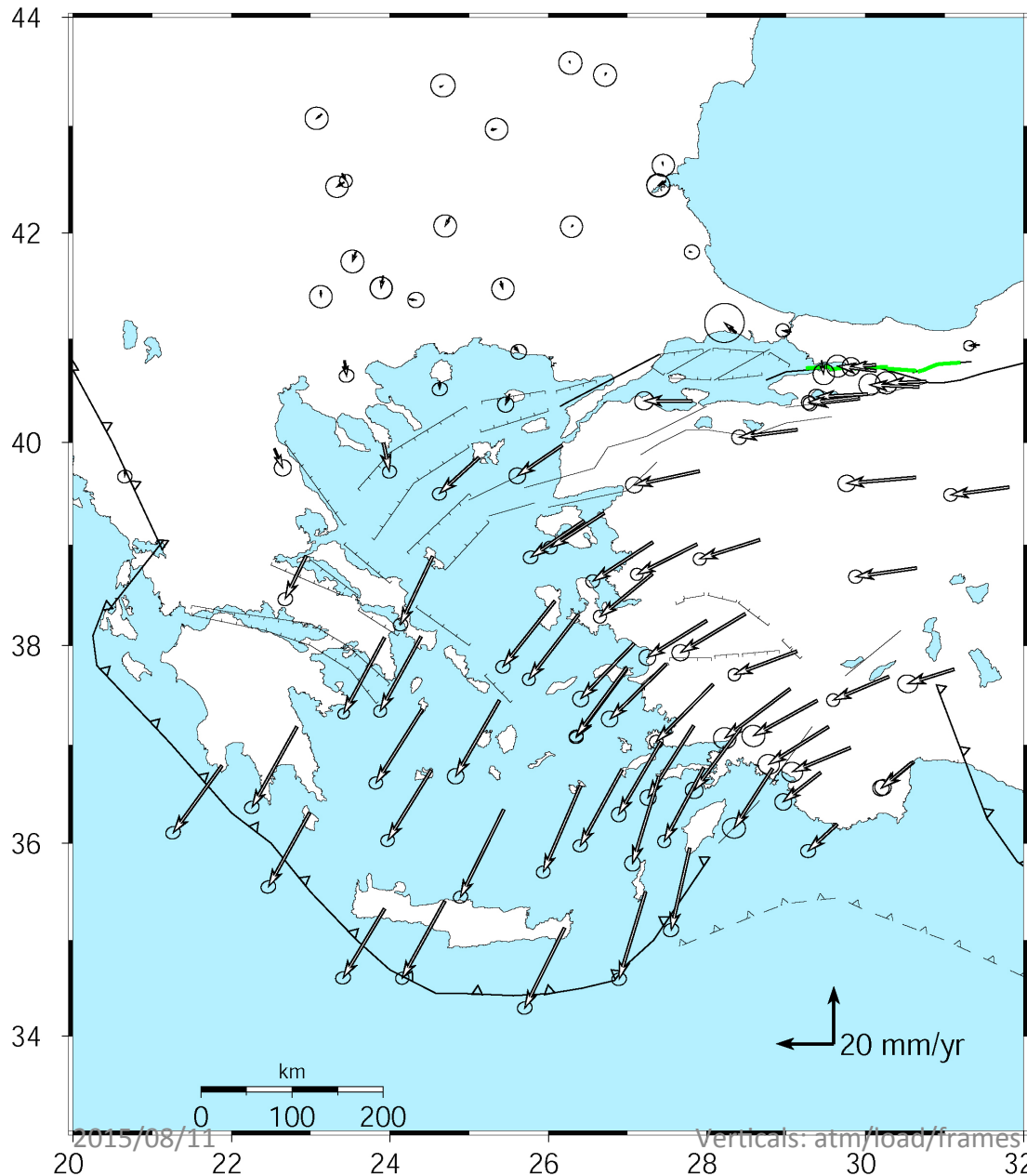
After stabilization, glorg will estimate a rotation vector ('Euler pole') for each plate with respect to the frame of the full stabilization set and print the relative poles between each set of plates

Use sh_org2vel to extract the velocities of all sites with respect to each plate



Velocities of Anatolia and the Aegean in a Eurasian frame

- Realized by minimizing the velocities of 12 sites over the whole of Eurasia



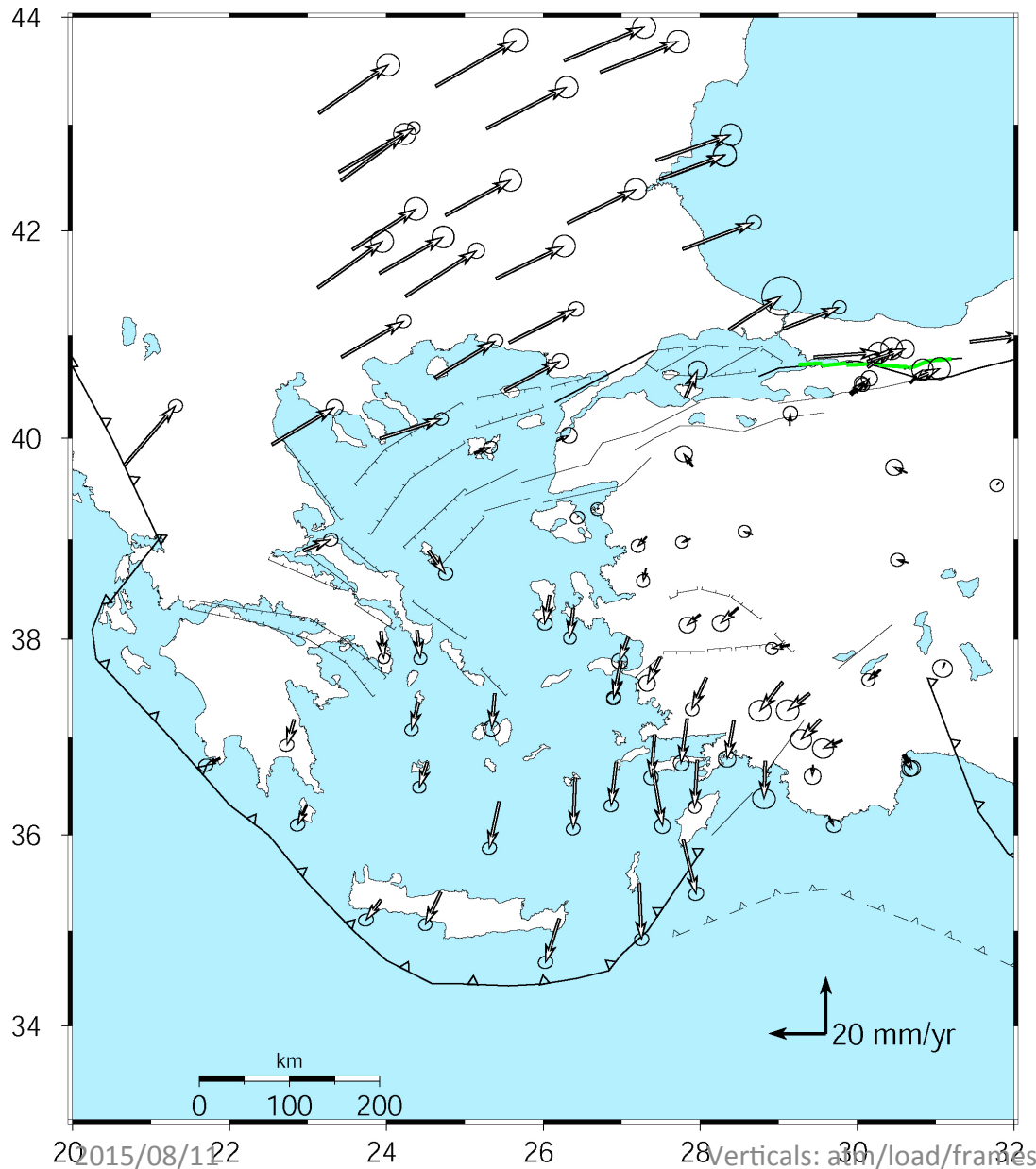
McClusky *et al.* [2000]

Velocities in an Anatolian frame

Better visualization of Anatolian and Aegean deformation

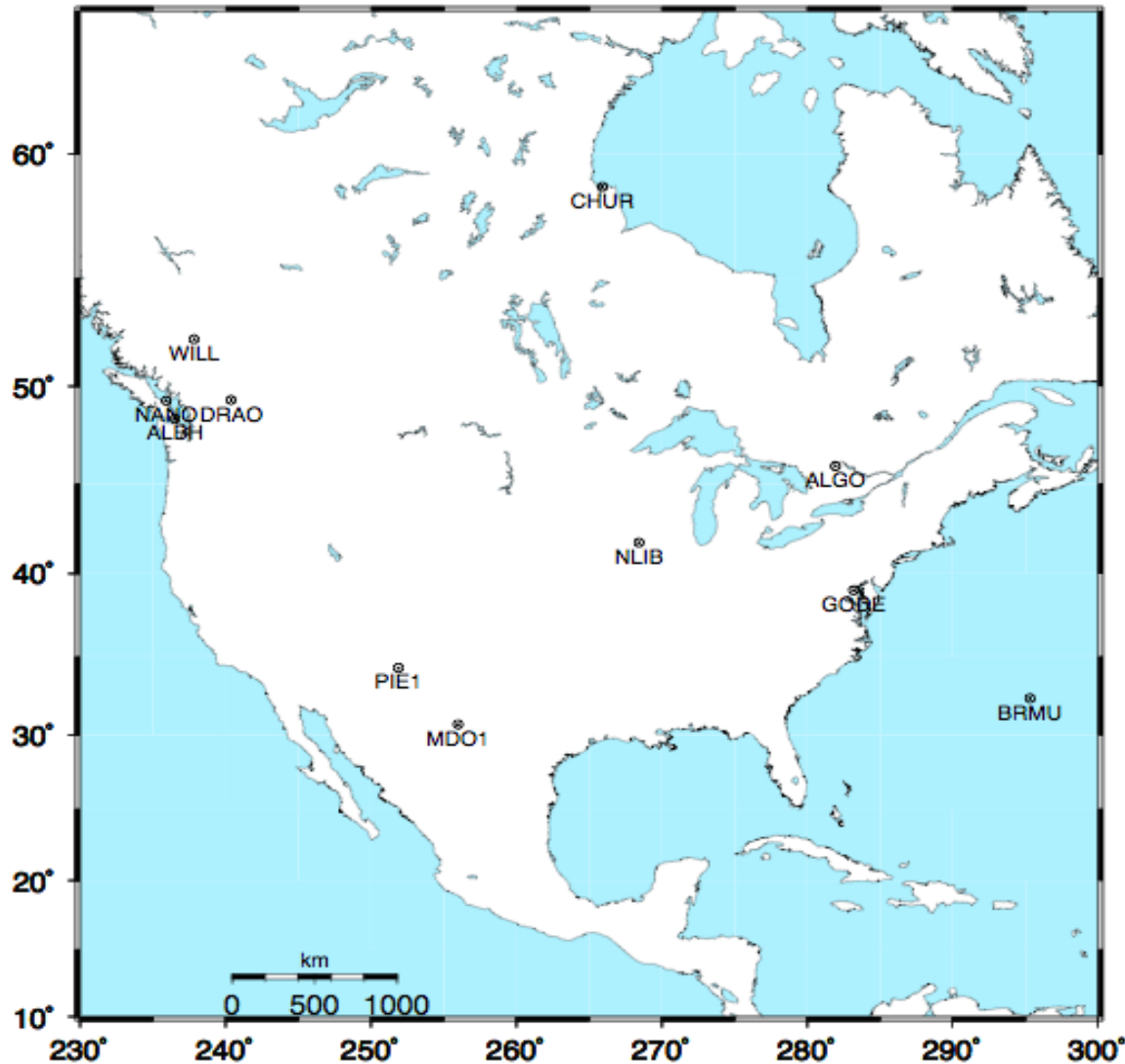
Here stations in Western/Central are used to align the reference frame (a priori velocity set to zero).

McClusky *et al.* [2000]

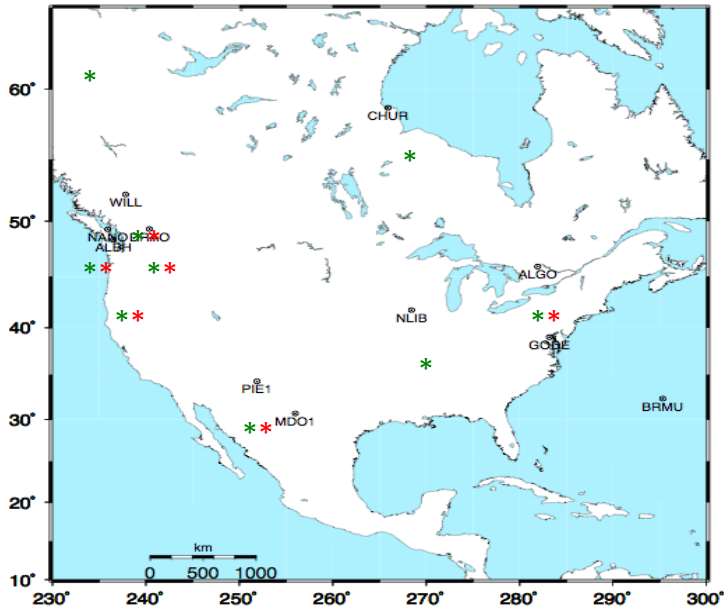


Stabilization Challenges for Time Series

Network too wide to estimate translation-only (but reference sites too few or poorly distributed to estimate rotation robustly)

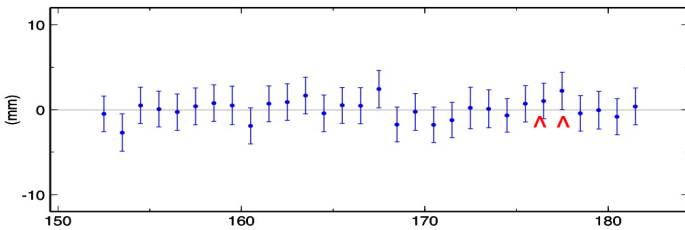


Stable reference frame



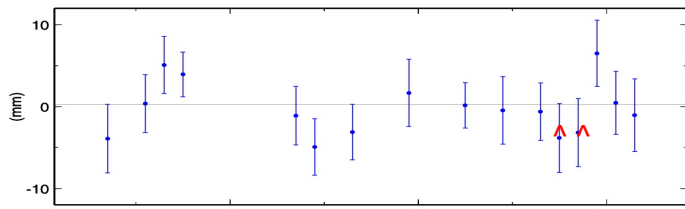
Example of time series for which the available reference sites changes day-to-day but is robust (6 or more sites, well distributed, with translation and rotation estimated)

DRAO North Offset 5490568.916 m
 $wmean(mm) = 8916.81 \pm 0.39$ $n rms = 0.54$ $w rms = 1.2$ mm # 30



Day 176 ALGO PIE1 DRAO WILL ALBH
 NANO rms 1.5 mm

BRMU North Offset 3603456.226 m
 $wmean(mm) = 6229.64 \pm 0.90$ $n rms = 0.91$ $w rms = 3.3$ mm # 16

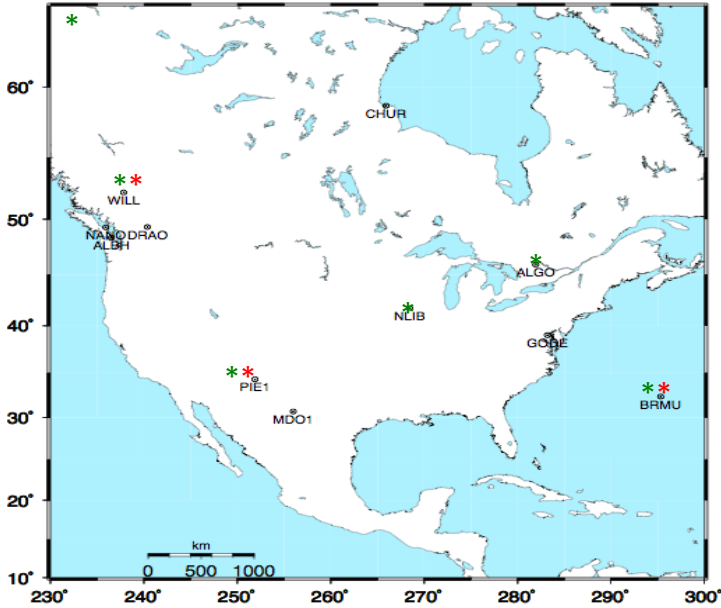


Day 177 ALGO NLIB CHUR PIE1 YELL DRAO
 WILL ALBH NANO
 rms 2.3 mm

2015/08/11

Verticals: atm/load/frames

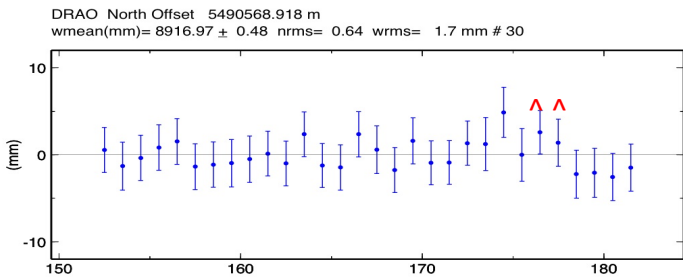
Unstable case



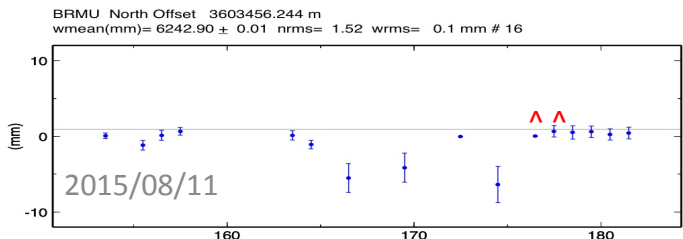
Example of time series for which the available reference sites changes day-to-day and is not robust (only 3 sites on one day)

NOTE: Distant frame definition sites can have very small error bars when used and large error bars when not used.

Day 176 BRMU PIE1 WILL
rms 0.4 mm



Day 177 BRMU ALGO NLIB PIE1
YELL WILL
rms 2.0 mm



Verticals: atm/load/frames

Rules for Stabilization of Time Series

- Small-extent network: translation-only in glorg, must constrain EOP in globk
- Large-extent network: translation+rotation, must keep EOP loose in globk;
- if scale estimated in glorg, it must estimate scale in globk
- 1st pass for editing:
 - “Adequate” stab_site list of stations with accurate a priori coordinates and velocities and available most days
 - Keep in mind deficiencies in the list
- Final pass for presentation / assessment / statistics
 - Robust stab_site list of all/most stations in network, with coordinates and velocities determined from the final velocity solution
- System is often iterated (velocity field solution, generate time series, editing and statistics of time series; re-generate velocity field).

GLOBK Reporting of models

- When binary h-files from GAMIT h-files are used (as opposed to SINEX files), GLOBK and GLIST can report models used. Can be critical when combining with MIT h-files.

```
GPS System Information : Time GPST Frame J2000 Precession
IAU76 Radiation model BERNE Nutation IAU00 Gravity EGR08
EarthRad NCLE1 AntThrust ANTBK
```

```
MODELS Used in Analysis: SD-WOB | SD-UT1 | IERS10 | E-
Tide | K1-Tide | PoleTide| OC-Load | MPT2010 | OceanPT |
```

```
LOAD Models Used : NCEP CM USED |
```

```
ATM Delay Models Used : UFL | GP25 | VMF1 | VMF1
| 2nd Order Ion | GMAP | IGRF11 |
```

These lines are wrapped.

Summary

- Atmospheric delay treatment and issues
 - VMF1 approach (used gridded assimilation meteorological data) is probably best but does require large and regularly updated (if near real-time) grid files
- Loading
 - Not standard yet in IGS processing. Again needs large grid files. Models used in GAMIT can be removed in GLOBK.
- Reference frame realization: Vertical effects
 - Treatment of scale estimates and impact on height estimates should be carefully considered when heights are of interest.